

ENSM Le Havre	DROITES DE HAUTEUR	V2.0 – 01/19
A. Charbonnel	CORRECTION - DROITES DE HAUTEUR NA	1/5

ATELIER 1 : CALCUL ET TRACÉ ELEMENTAIRES DE DROITES DE HAUTEUR

Exercice 1.1 - Drawing Line of position on plotting sheet

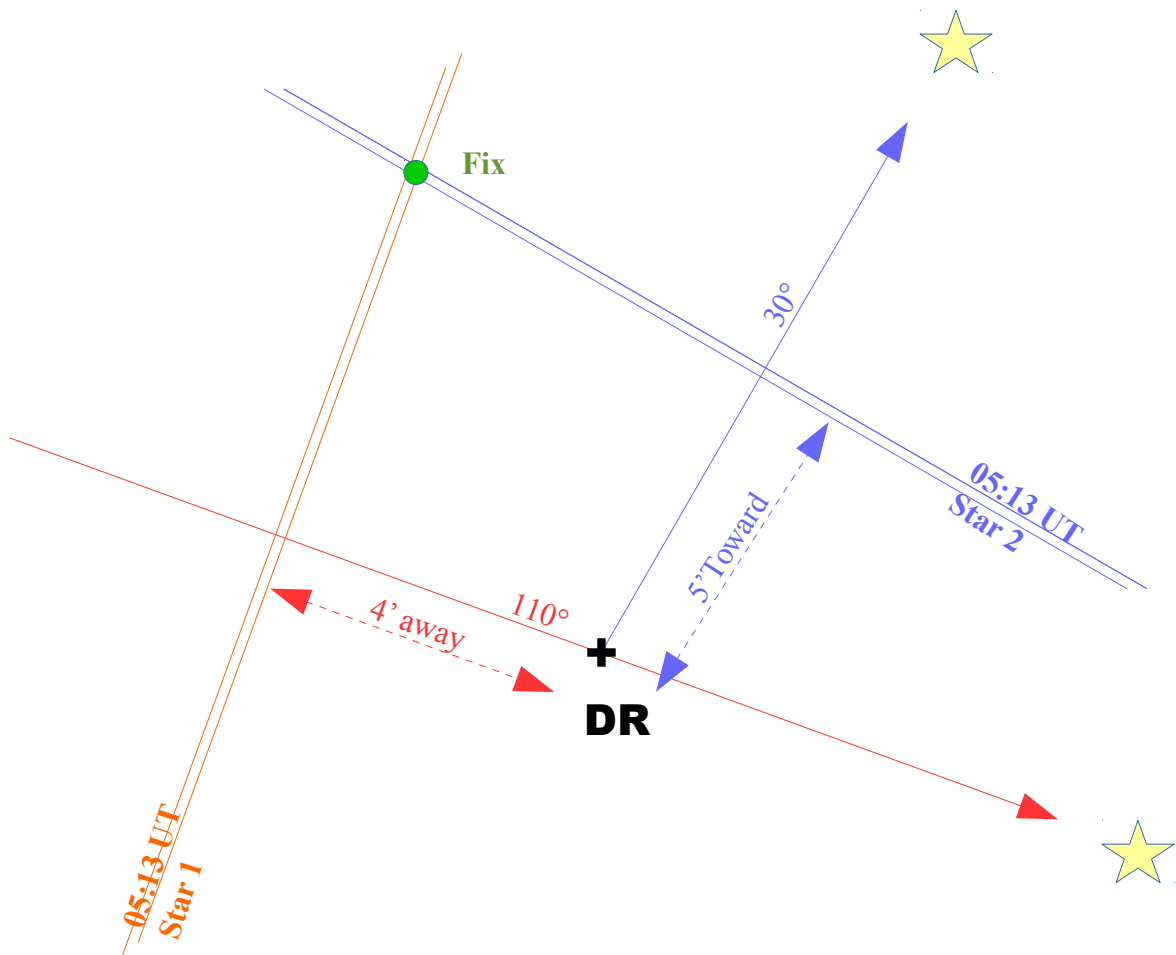
At 05h13min, DR position, $19^{\circ}20' N$, $116^{\circ}50' E$., two observations of stars were taken as follows:

- Star 1 - Bearing $110^{\circ} T$, intercept $4'$ away.
- Star 2 - Bearing $030^{\circ} T$, intercept $5'$ toward.

Find the ship's position

Correction partielle

Ce tracé est à faire sur un plotting sheet pour lire la position (latitude/longitude) du point



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Exercice 1.2 – Sight seeing reduction/ LOP with stars

Correction partielle

In the evening, 17th July 1981, at DR position $40^{\circ} 25'N$, $32^{\circ} 40'W$, the chronometer showed 10h 21min 07s, chronometer error 4min 09s fast.
 Observed Star Dubhe with sextant altitude $43^{\circ} 32,0'$ and star Deneb with sextant altitude $38^{\circ} 12,3'$; index error 2,3' on the arc; height of eye 15 m.
 Find intercepts and positions lines.

Define GMT

Chronometer Time	10h 21min 07s	
Chronometer Error	- 4min 09s	Fast - / Slow +
Time GMT [12h]	10h 16min 58s	
GMT	22h 16min 58s	Time on 24h

Intercept for Dubhe

Define LHA* et D* for Dubhe

GHA γ	$265^{\circ} 38,0'$	NA - à l'heure ronde = 22h00	
+ Δ GHA γ	$4^{\circ} 15,2'$	Pour $\Delta t = 156\text{min } 58\text{s}$	
= GHA γ	$269^{\circ} 53,2'$	À l'heure précise = 22h 15min 58s	
+ SHA*	$194^{\circ} 21,9'$	NA	D* = $61^{\circ} 51,4'N$
GHA*	$104^{\circ} 15,1'$	$464^{\circ} 15,1' [360]$	
- Ge	- $32^{\circ} 40,0'$		
LHA*	$71^{\circ} 35,1'$		

Calculate hc

$$\begin{aligned} \sin h_c &= \sin \phi_e \cdot \sin D + \cos \phi_e \cdot \cos D \cdot \cos LHA \\ &= \sin(40^{\circ} 25') \cdot \sin(61^{\circ} 51,4') + \cos(40^{\circ} 25') \cdot \cos(61^{\circ} 51,4') \cdot \cos(71^{\circ} 35,1') \\ &= 0,685 \\ \rightarrow h_c &= 43^{\circ} 14,7' \end{aligned}$$

$$\mathbf{Hc = 43^{\circ} 14,7'}$$

Calculate Zc

$$\begin{aligned} \cos AZ_c &= \frac{\sin D - \sin \phi_e \cdot \sin h_c}{\cos \phi_e \cdot \cos h_c} \\ &= \frac{\sin(61^{\circ} 51,4') - \sin(40^{\circ} 25') \cdot \sin(43^{\circ} 14,7')}{\cos(40^{\circ} 25') \cdot \cos(43^{\circ} 14,7')} \approx 0,78901 \\ \rightarrow AZ_c &\approx 38^{\circ} \\ LHA &= 71^{\circ} 35,1' \rightarrow Z_c = 360^{\circ} - AZ_c \end{aligned}$$

$$\mathbf{Zc = 322^{\circ}}$$

Calculate ho

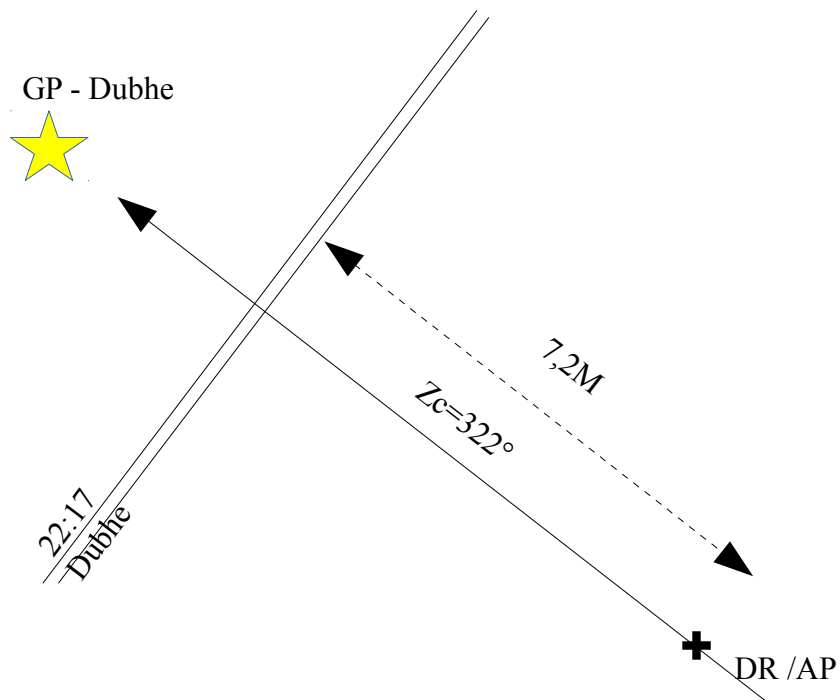
hs	43°32,0'
+ IC	-2,3'
+ Dip	-6,8'
ha	43° 22,9'
+Alt. Main correction	-1,0'
-30' for upper limb (Moon)	
+U,L, correction for Moon	
+Additional correction for Venus	
+Additional refraction correction (non standard Temp/pression)	
ho	43°21,9'

Calculate the intercept/LOP

ho	43°21,9'	
- hc	- 43° 14,7'	
= i	+ 7,2'	Zc= 322°

Draw the LOP

XDD



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Exercice 1.3 – Sight seeing reduction / LOP with the SUN

At 0900 LMT, 25th October 1981, DR position 43°15' N, 38°25' W, the chronometer shows 11h 40min 32s, chronometer error is 2m 20s slow.
Sextant altitude of the sun's lower limb is 24°02.3' ; index error 1.5' off the arc; height of eye 12 m.
Find intercept and position line:

Define GMT

Ge/15 = 2h 33min 40s

Chronometer Time	11h 40min 32s	Approx LMT	09h00
Chronometer Error	2min 20s	Fast - / Slow +	+ Ge 2h 33min 40s
Time GMT [12h]	11h 42min 52s	Approx GMT	11h 33 min 40s
GMT	11h 42min 52s	Time on 24h	

Define LHA/GHH et D

GHA _a	348° 58,5'	NA - à l'heure ronde = 11h00	D	12° 09' S
+ΔGHA _a	10° 43,0'	Pour Δt = 42min 52s / d=0,9	+ΔD	+ 06'
= GHA _a	359° 41,5'	À l'heure précise = 22h 15min 58s	D	12° 15' S
- Ge	- 38° 25,0'			
LHA_a	321° 16,5'			

Calculate hc

$$\begin{aligned} \sin h_c &= \sin \phi_e \cdot \sin D + \cos \phi_e \cdot \cos D \cdot \cos LHA \\ &= \sin(43^\circ 15') \cdot \sin(-12^\circ 15') + \cos(43^\circ 15') \cdot \cos(-12^\circ 15') \cdot \cos(321^\circ 16,5') \\ &= 0,4099 \\ \rightarrow h_c &= 65^\circ 48,0' \end{aligned}$$

$$H_c = 65^\circ 48,0'$$

Calculate Zc

$$\begin{aligned} \cos AZ_c &= \frac{\sin D - \sin \phi_e \cdot \sin h_c}{\cos \phi_e \cdot \cos h_c} \\ &= \frac{\sin(-12^\circ 15') - \sin(43^\circ 15') \cdot \sin(65^\circ 48')}{\cos(43^\circ 15') \cdot \cos(65^\circ 48')} \approx -0,0295' \\ \rightarrow AZ_c &\approx 91,5^\circ \\ LHA - \text{astre à l'est} &\rightarrow Z_c = AZ_c = 91,5^\circ \end{aligned}$$

$$Z_c = 91,5^\circ$$

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Calculate ho

hs	24°02,3'
+ IC	+ 1,5'
+ Dip	-6,8'
ha	43° 22,9'
+Alt. Main correction	-1,0'
-30' for upper limb (Moon)	
+U,L, correction for Moon	
+Additional correction for Venus	
+Additional refraction correction (non standard Temp/pression)	
ho	43°21,9'

Calculate the intercept/LOP

ho	43°21,9'	
- hc	- 43° 14,7'	
= i	+ 7,2'	Zc= 322°

Draw the LOP

ATELIER 2 : TRANSPORT DE DROITES

ATELIER 3 : PROBLEMES DIVERS

